

FIELD FLATNESS OF DOUBLER DIPOLES

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December 20, 1979

I. Introduction

Acceptance criteria for the field quality of doubler dipoles have been set up for multipole components up to and including the decapole. In addition, criteria for $|\Delta B_{\hat{Y}}/B_{\hat{O}}|$ and $|B_{\hat{X}}/B_{\hat{O}}|$ on the median plane at $x=\pm 0.5$ and ± 1 have been in use so far. These criteria on the overall flatness of dipoles are based on a purely pragmatic reasoning and do not come from requirements of beam dynamics. If a dipole satisfied all criteria on multipole components but did not meet the flatness criteria, this magnet would be installed at a place where both β_h and the momentum dispersion parameter are small. The practice up to now has been to be firm but flexible and reasonable in judging each magnet for the final acceptance. Admittedly, the procedure is partially subjective and the final decision inevitably depends on many factors.

The question of field flatness has been brought up by Alvin Tollestrup and Tom Collins recently and there was a meeting (December 11th) to discuss this somewhat ambiguous matter. It was clear (to me at least) that they entertained a possibility of momentum stacking in addition to the desirability of having a flexibility to move the beam in and out. Once we start taking this seriously, we may have to reevaluate the correction system or we may have to demand doubler dipoles of much better field quality. Neither prospect is a welcome thing for us at this time and the final decision can be made only by the PMG. The purpose of this note is to present available data on the question of flatness or, equivalently, data on the <u>local</u> multipole fields. After some discussions at the meeting on December 11th, it was more or less agreed that we should look at the field errors at ±0.8" and the local field gradients at ±0.5".

In evaluating the field, the contributions from the quadrupole (normal and skew) and the normal sextupole components will not be included since they are expected to be compensated for by the correction system,

$$b_1 = b_2 = a_1 = 0$$
.

The momentum stacking proposed by T. Collins^{1,2} expects $\Delta p/p = \pm 0.2\%$ with the maximum value of dispersion parameter at around 10 m. Therefore, the beam can be at $x = \pm 0.8$ " but the average radial beam position in dipoles will be $3m \times (\pm 0.2\%) \approx \pm 0.25$ ".

It is difficult to define the boundary of the area within the bore tube in which the beam should survive. If the momentum stacking is the only consideration, one would look at local field errors, local field gradients and, possibly, local sextupole fields within $x \approx \pm 0.3$ " and y ~±0.15". For this case, skew sextupole and octupole fields will be the dominant components and the addition of corresponding correction system will improve the field substantially. If the area of our interest extends to $x = \pm 0.8$ ", higher-order natural multipoles (14-poles, 18poles, etc.) will make significant contributions and one may get the impression that the addition of skew sextupole or normal octupole correction system makes very little difference. One may even begin to contemplate a correction system which is not based on the multipole decomposition (something similar to the ISR system). The "proper" value of y is even more difficult to decide. Ordinarily, one would not think of a closed orbit which is displaced vertically by 0.5"; if one must consider the stability of such an orbit, many new problems would come up and the whole thing is likely to be an entirely new ball game. I mention these points before presenting data so that we are all aware of pitfalls associated with the interpretation of data. If a decision to do (or not to do) something is to be made based on the data, that decision must necessarily be of a soul-searching nature.

II. Data

Data from forty-one dipoles have been used and the dipoles are:

1.	accepted (16)			211 235					224	226
2.	rejected (6)	200	218	219	221	223	239			
3.	undecided (13)			216 254		220	237	243	244	245
4.	long cryostat (6)	202	203*	204	205	206	208			

*TA0203 is counted twice, with a long and a short cryostat.

normal field:
$$b_{y} \equiv (B_{y} - B_{o})/B_{o} \quad \text{in } 10^{-4}$$
skew field:
$$b_{x} \equiv B_{x}/B_{o} \quad \text{in } 10^{-4}$$
normal gradient
$$b_{y}' \equiv \partial b_{y}/\partial x \quad \text{in } 10^{-4}/\text{inch}$$
skew gradient
$$b_{x}' \equiv \partial b_{x}/\partial x \quad \text{in } 10^{-4}/\text{inch}$$

All data are at (nominal) 4,000A and $b_1=b_2=a_1=0$ is always assumed. It is possible to accumulate many tables and figures but the following cases are presented here:

- Table 1. $x = \pm 0.8$ ", y = 0 with and without correction for a_2 (skew sextupole field); 41 dipoles.
- Table 2. same as Table 1, 16 accepted dipoles only.
- Table 3. $x = \pm 0.5$ ", y = 0, otherwise same as Table 1.
- Table 4. same as Table 3, 16 accepted dipoles only.
- Table 5. $x = \pm 0.5$ ", $y = \pm 0.25$ ", otherwise same as Table 1.
- Table 6. same as Table 5, 16 accepted dipoles only.
- Table 7. $x = \pm 0.3$ ", y = 0; effects of b_3 , b_4 , a_2 , a_3 and a_4 ; 41 dipoles.
- Table 8. same as Table 7, 16 accepted dipoles only.

Quantities listed in each row are:

- 1. average value
- 2. standard deviation
- 3. number of magnets beyond one standard deviation
- 4. number of magnets beyond two standard deviations

III. Comments

Tom Collins commented that, in establishing criteria on the field flatness, there should be some guidelines based on the beam dynamics instead of relying exclusively on pragmatic considerations. If the ideal closed orbit with $\Delta p/p \neq 0$ is considered to be on the median plane (y = 0), effects of b_y , b_x , $\partial b_y/\partial x$ and $\partial b_x/\partial x$ on the closed orbit can be estimated in the conventional manner. It will be particularly instructive to compare the field quality at various values of $x \neq 0$ (with the correction $b_1 = b_2 = a_1 = 0$) with the field quality at x = 0 without any correction.

1) average b_v

This shifts the closed orbit as a whole radially. The effect is very small even at $x = \pm 0.8$ ".

2) average b_x

With $b_x = 1$, the maximum vertical excursion of the orbit is 0.68mm and the rms excursion is 0.34mm. The effect is negligible since $|(b_x)_{av}| < 0.7$ for |x| < 0.8".

3) fluctuations in b_{x} and b_{x}

Expected closed-orbit distortions are (assuming v = 19.4)

radial:
$$\langle \Delta x \rangle = 9.0 \text{m} \times \langle b_{\text{v}} \rangle$$
 at $\beta_{\text{h}} = 100 \text{m}$,

vertical:
$$\langle \Delta y \rangle = 9.1 \text{m} \times \langle b_y \rangle$$
 at $\beta_y = 100 \text{m}$.

By taking twice the rms value, one can probably gain (80 -85)% confidence level. The distortions may not be entirely negligible at $x = \pm 0.8$ " but

they are certainly very small at $x = \pm 0.5$ " or less.

4) average $\partial b_y/\partial x$

The corresponding parameter at x=0 is b_1 (normal quadrupoles) and it is approximately - 1 (without any correction). It is possible that the average value of $\partial b_y/\partial x$ would change somewhat as we continue to accumulate the dipoles. Nevertheless, the tune shifts are large at |x| > 0.5". They are safe at $x = \pm 0.3$ ".

$$\Delta v_{x} = 0.11 \times (\partial b_{y}/\partial x)_{av}$$
, $\Delta v_{y} = -0.12 \times (\partial b_{y}/\partial x)_{av}$

5) fluctuation in $\partial b_{V}/\partial x$

This drives the resonances $2v_x = n$ and $2v_y = n$. At x = 0 without any correction,

$$(\partial b_y/\partial x)_{std.dev.}$$
 $(b_1)_{std.dev.} = 1.47 \text{ (at 4,000A)}$

The corresponding full resonance width (rms) is 0.013. This is similar to the situation at $x = \pm 0.5$ " with the correction for b_1 , b_2 (a_1 is immaterial). With y = 0.25", the width becomes twice as large.

6) average $\partial b_{y}/\partial x$

This drives the resonance v_x - v_y = 0. At x = 0 without any correction,

$$(\partial b_x/\partial x)_{av} \rightarrow (a_1)_{av} = -0.27 (500A) \text{ to } 0.12 (4,000A)$$

Although there will be a sizable coupling even at $x = \pm 0.3$ ", this resonance by itself should not be too harmful to the beam.

7) fluctuation in $\partial b_{y}/\partial x$

This drives the resonance $v_x + v_y = n$. At x = 0 without any correction,

$$(\partial b_x/\partial x)_{std. dev.} \rightarrow (a_1)_{std. dev.} = 1.9 (4,000A)$$

Again this is more or less what we have at $x = \pm 0.5$ " with the correction for a_1 (b_n corrections immaterial).

The impression one gets from these data is that the beam will survive if the closed orbit is confined to |x| < 0.3" and |y| < 0.2". If we are lucky, this may be extended to $|x| \approx 0.5$ " but definitely not more than that. From Tables 7 and 8, one sees that the addition of skew sextupole correction alone cannot extend the area. Order=of-magnitude improvements are possible with b₄ (normal decapole) and a₃ (skew octupole) corrections. This is more than I anticipated in the Introduction.

References

- 1. T. L. Collins, UPC No. 23, December 13, 1978.
- 2. "A Report on the Design of the Fermi National Accelerator Laboratory Superconducting Accelerator", May 1979, 182 183.
- 3. S. Ohnuma, TM-910, October 15, 1979.

Table 1. $x = \pm 0.8$ ", y = 0; with and without correction for a_2 (skew sextupoles); 41 dipoles.

a ₂ ≠ 0	$a_2 = 0$
SAMPLE NUMBER = 41	SAMPLE NUMBER = 41
X % Y: 0.80 0.00 INCH BY: -0.5255 0.8709 14 2 BX: -0.6544 1.4883 8 3 BYP: -8.7114 4.2241 16 3 BXP: -1.5425 5.6659 10 3	X % Y: 0.80 0.00 INCH BY: -0.5255 0.8709 14 2 BX: -0.2870 1.3205 10 2 BYP: -8.7114 4.2241 16 3 BXP: -0.6240 5.4193 12 2
a ₂ ≠ 0 SAMPLE NUMBER = 41	a ₂ = 0 SAMPLE NÚMBER = 41
X & Y: -0.80 0.00 INCH BY: 0.0999 1.0045 15 2 BX: -0.2103 1.6476 10 2 BYP: 5.9670 4.7322 16 1 BXP: 0.7046 6.0797 10 3	X % Y: -0.80 0.00 INCH BY: 0.0999 1.0045 15 2 BX: 0.1570 1.3885 9 2 BYP: 5.9670 4.7322 16 BXP: -0.2139 5.6254 9 2

Table 2. same as Table 1, 16 accepted dipoles only.

$a_2 \neq 0$	$a_2 = 0$			
SAMPLE NUMBER = 16	SAMPLE NUMBER = 16			
X & Y: 0.80 0.00 INCH BY: -0.3135 0.9204 4 0 BX: -0.4911 1.7212 3 1 BYP: -7.6025 4.2998 5 0 BXP: -1.0746 6.3235 6 1	X % Y: 0.80 0.00 INCH BY: -0.3135 0.9204 4 0 BX: -0.3177 1.3771 5 1 BYP: -7.6025 4.2993 5 0 BXP: -0.6411 5.6209 6 1			
a ₂ ≠ 0	$a_2 = 0$			
SAMPLE NUMBER = 16	SAMPLE NUMBER = 16			
X & Y: -0.80	X & Y: -0.80 0.00 INCH BY: 0.1470 0.8701 5 1 BX: 0.2959 1.4159 3 1 BYP: 5.7168 4.2143 5 0 BXP: -0.8637 5.7970 3 1			

Table 3. $x = \pm 0.5$ ", y = 0; with and without correction for a_2 (skew sextupoles); 41 dipoles.

a ₂ ≠ 0	$a_2 = 0$
SAMPLE NUMBER = 41	SAMPLE NUMBER = 41
X & Y: 0.50 0.00 INCH BY: 0.0308 0.1524 14 2 BX: -0.2215 0.4079 8 3 BYP: 0.3213 1.1078 16 2 BXP: -1.0667 2.1446 8 3	X & Y: 0.50 0.00 INCH BY: 0.0308 0.1524 14 2 BX: -0.0780 0.3028 9 2 BYP: 0.3213 1.1078 16 2 BXP: -0.4927 1.8570 10 2
a ₂ ≠ 0	$a_2 = 0$
SAMPLE NUMBER = 41	SAMPLE NUMBER = 41
X & Y: -0.50 0.00 INCH BY: 0.1618 0.1789 14 2 BX: -0.0911 0.4565 12 3 BYP: -1.1595 1.2937 15 1 BXP: 0.2810 2.3986 10 2	X & Y: -0.50 0.00 INCH BY: 0.1618 0.1789 14 2 BX: 0.0524 0.3162 9 BYP: -1.1595 1.2937 15 BXP: -0.2931 1.9570
Table 4. same as Table 3,	16 accepted dipoles only.
a ₂ ≠ 0 SAMPLE NUMBER = 16	a ₂ = 0 SAMPLE NUMBER = 16
X % Y: 0.50 0.00 INCH BY: 0.0674 0.1690 5 0 BX: -0.1565 0.4798 3 1 BYP: 0.5800 1.1991 4 0 BXP: -0.8249 2.5127 3 1	<pre></pre>
a ₂ ≠ 0 SAMPLE MUMBER = 16	a ₂ = 0 SAMPLE NUMBER = 16
X % Y: -0.50	X & Y: -0.50 0.00 INCH BY: 0.1647 0.1522 5 1 BX: 0.0768 0.3226 2 1 BYP: -1.2119 1.0960 5 1 BXP: -0.4687 1.9865 2

Table 5. $x = \pm 0.5$ ", y = 0.25"; with and without correction for a_2 (skew sextupoles); 41 dipoles.

a ₂ ≠ 0	a ₂ = 0
SAMPLE NUMBER = 41	SAMPLE NUMBER = 41
X % Y: 0.50 0.25 INCH BY: 0.1614 0.5040 9 2 BX: 0.0165 0.3007 14 3 BYP: 1.3501 2.0880 12 3 BXP: 0.8894 2.2118 9 3	X % Y: 0.50 0.25 INCH BY: 0.0179 0.4218 10 BX: 0.1241 0.2419 13 BYP: 1.0631 1.9954 11 BXP: 1.4635 1.9935 12
a ₂ ≠ 0	a ₂ = 0
SAMPLE NUMBER = 41	SAMPLE NUMBER = 41
X % Y: -0.50	X % Y: -0.50 0.25 INCH BY: -0.0095 0.4479 8 BX: -0.2915 0.2656 14 BYP: -1.2212 2.1432 9 BXP: 2.4465 2.1867 14

Table 6. same as Table 5, 16 accepted dipoles only.

$a_2 \neq 0$	$a_2 = 0$
SAMPLE NUMBER = 16	SAMPLE NUMBER = 16
X % Y: 0.50 0.25 INCH BY: 0.0976 0.5950 3 1 BX: 0.1227 0.3342 3 0 BYP: 1.3914 2.4120 4 1 BXP: 1.4400 2.5178 3 1	X & Y: 0.50 0.25 INCH BY: 0.0299 0.4559 2 BX: 0.1735 0.2535 5 BYP: 1.2560 2.1986 4 BXP: 1.7109 2.0872 5 1
a ₂ ≠ 0 SAMPLE NUMBER = 16	a ₂ = 0 SAMPLE NUMBER = 16
X & Y: -0.50	X & Y: -0.50

$b_1,b_2,b_3,b_4,a_1=0$ SAMPLE NUMBER = 41	X & Y: 0.30 0.00 INCH BY: 0.0037 0.0010 13 2 BX: -0.0671 0.1192 7 3 BYP: 0.0688 0.0169 14 2 BXP: -0.5062 0.9213 8 3	$b_1,b_2,a_1,a_2,a_3,a_4=0$ X & Y: 0.30 0.00 INCH E Y: -0.00032 0.0260 16 1 B X: -0.0004 0.0019 15 2 B YP: 0.0193 0.2922 16 1 B XP: -0.0063 0.0316 15 2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
$b_1,b_2,b_3,a_1=0$ SHMPLE NUMBER = 41	X & Y: 0.30 0.00 INCH BY: 0.0096 0.0164 17 1 BX: -0.0671 0.1192 7 3 BYP: 0.1469 0.2180 17 1 BXP: -0.5062 0.9213 8 3	b ₁ ,b ₂ ,a ₁ ,a ₂ ,a ₃ = 0 × & Y: 0.30 0.00 INCH BY: -0.0032 0.0260 16 1 BX: -0.0020 0.0044 10 2 BYP: 0.0193 0.2922 16 1 BXP: -0.0276 0.0626 10 2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
b_1 , b_2 , $a_1=0$ SAMPLE NUMBER = 41	X % Y: 0.30 0.00 INCH BY: -0.0032 0.0260 16 1 BX: -0.0671 0.1192 7 3 BYP: 0.0193 0.2922 16 1 BXP: -0.5062 0.9213 8 3	$b_1,b_2,a_1,a_2=0$ $X & Y: 0.30 0.00 INCH$ $BY: -0.0032 0.0260 16 1$ $BX: -0.0154 0.0644 8 3$ $BYP: 0.0193 0.2922 16 1$ $BXP: -0.1618 0.6468 8 3$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

effects of higher-multipole corrections. x = (0.3", y = 0;Table 7.

41 dipoles.

$b_1,b_2,b_3,b_4,a_1=0$ SAMPLE NUMBER = 16	X & Y: 0.30 0.00 INCH BY: 0.0037 0.0009 4 1 BX: -0.0423 0.1357 3 1 BYP: 0.0678 0.0160 5 1 BXP: -0.3482 1.0821 3 1	$b_1,b_2,a_1,a_2,a_3,a_4=0$ \times & Y: 0.30 0.00 INCH BY: 0.0031 0.0295 5 1 BX: -0.0007 0.0022 6 0 BYP: 0.0902 0.3283 5 0 BXP: -0.0110 0.0367 6 0	b ₁ ,b ₂ ,b ₃ ,b,	0013 1065 0230 8385	$b_{\perp}, b_{2}, a_{1}, a_{2}, a_{4} = 0$ $x \in Y$: -0.30 0.00 INCH BY: 0.0224 0.0265 5 1 BX: 0.0006 0.0021 6 0 BYP: -0.2900 0.2931 5 1 BXP: -0.0097 0.0354 6 0
$b_1, b_2, b_3, a_1 = 0$ SAMPLE NUMBER = 16	X % Y: 0.30 0.00 INCH BY: 0.0122 0.0149 5 0 BX: -0.0423 0.1357 3 1 BYP: 0.1818 0.1987 5 0 BXP: -0.3482 1.0821 3 1	$b_1,b_2, a_1,a_2,a_3=0$ $\times \& Y: 0.30 0.00 INCH$ $BY: 0.0031 0.0295 5 1$ $BX: -0.0014 0.0053 4 0$ $BYP: 0.0902 0.3283 5 0$ $BXP: -0.0213 0.0751 4 0$	$b_1, b_2, b_3, a_1 = $	BY: 0.0132 0.0147 5 1 BX: -0.0081 0.1065 3 1 BYP: -0.1984 0.1946 5 1 BXP: -0.0011 0.8385 4 1	$b_1,b_2,a_1,a_2,a_3=0$ $X \& Y! = -0.30$ 0.00 INCH $BY!$ 0.0224 0.0265 5 1 $BX!$ -0.0002 0.0044 4 1 $BYP!$ -0.2900 0.2931 5 1 $BXP!$ 0.0007 0.0609 4 1
$\mathrm{b_1,\ b_2,\ a_1=0}$ shmple mumber = 16	X % Y: 0.30 0.00 INCH BY: 0.0031 0.0295 5 1 BX: -0.0423 0.1357 3 1 BYP: 0.0902 0.3283 5 0 BXP: -0.3482 1.0821 3 1	$b_1,b_2,a_1,a_2=0$ $X \& Y: 0.30 0.00 INCH$ $\& BY: 0.0031 0.0295 5 1$ $\& BXP: 0.0902 0.3283 5 0$ $\& BXP: -0.1856 0.6808 3 1$	b ₁ , b ₂ , Y: -0.30	BY: 0.0224 0.0265 5 1 BX: -0.0081 0.1065 3 1 BYP: -0.2900 0.2931 5 1 BXF: -0.0011 0.8385 4 1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

effects of higher-multipole corrections. $x = \pm 0.3$ ", y = 0; effective accepted dipoles only. Table 8.



Addendum to "FIELD FLATNESS OF DOUBLER DIPOLES"

S. Ohnuma December 27, 1979

The second meeting to discuss the subject was held on December 21st. Although the importance of normal decapole and skew octupole was generally recognized, there was no conclusion as to what we should do to enlarge the usable aperture of dipoles. Since the condition $b_4=a_3=0$ cannot be realized with the addition of correction magnets, the desirability of making detailed numerical computations with a realistic correction system became clear during the discussion. The computer program developed by Al Russell can handle the problem and any decision on our future plans should be made after his results became available.

The purpose of this addendum is to supplement the statistical information given in UPC No. 118 in order to clarify two questions raised in the second meeting. The first is the field quality of the ideal dipole ("Snowdon dipole") and the second is the improvement one can expect from the b_A and a_3 corrections beyond 0.3".

A. Ideal Dipoles

The following numbers are based on the information given in the Design Report (May 1979), p. A23, "Integrated Multipole Structure of E-Series Dipole", calculation mode = 1:

$$b_2 = 0.039$$
 $b_4 = 1.037$ $b_6 = 4.435$ $b_8 = -12.09$ $b_{10} = 3.634$ $b_{12} = -0.822$ $b_{14} = 0.069$ $b_{16} = 0.031$ $b_{18} = -0.044$

The unit for b_n is $10^{-4}/(inch)^n$.

 $a_n = b_{2n+1} = 0$

Multipoles are apparently chosen such that the "flat" field extends to ~ 0.8 ". In achieving this, the nonlinear field ΔB_y (y=0) is made to vanish at |x| = 0.78" by balancing contributions from various multipoles. The local gradient $\partial B_y/\partial x$ on the median plane, which is an odd function of x, is positive for x < 0.66" and negative beyond that. As a consequence, if one is interested in the field and the gradient for |x| < 0.5", the contribution from b_4 (which is designed to be non-zero) to the local gradient is not entirely negligible and one would rather like to have $b_4 = 0$. Fig. 1 shows ΔB_y and $\partial B_y/\partial x$ on the median plane with $b_4 = 1.04 \times 10^{-4}/in^2$ and with $b_4 = 0$. For example, at x = 0.5",

if
$$b_4 = 1.04 \times 10^{-4}/in^2$$
, $\partial B_y/\partial x = 0.70 \times 10^{-4} B_0/in$, $\Delta v = \pm 0.08$ if $b_4 = 0$, $\partial B_y/\partial x = 0.18 \times 10^{-4} B_0/in$, $\Delta v = \pm 0.02$.

Beyond $|\mathbf{x}|=0.62$ ", the ideal dipole is superior to the one with $\mathbf{b_4}=0$ if the resulting Δv is used as the criterion. If $|\Delta \mathbf{B_Y}|$ is used, it is better beyond $|\mathbf{x}|=0.73$ ". Presumably, as we accumulate dipoles, the average value of $\mathbf{b_4}$ will approach the design value*. If the game is to improve the field quality for $|\mathbf{x}|<0.6$ ", one may conclude that a correction system is needed to make $\mathbf{b_4}=0$. On the other hand, the spirit of the design, which is completely justifiable, was to make the field flat as much as possible to $|\mathbf{x}|\simeq0.8$ " and $\mathbf{b_4}=1.04$ is a consequence of this design philosophy. I must again emphasize the point that, unless we have a definite idea on what we want, arguments on the field flatness will be meaningless. One cannot play a game without knowing its rules.

B. Improvement with $b_4 = 0$ and $a_3 = 0$ beyond 0.3"

Fig. 2A. average value of $\Delta B_{Y}(y=0)$ There is no effect coming from $b_4=0$. Note that, up to 0.7",

^{*} For 16 accepted dipoles, $(b_4)_{av} = 1.334(500A)$, 1.312(1,000A), and 1.056(4,000A).

 $(\Delta B_{y})_{ay}$ is <u>less</u> than what one should expect from the ideal dipole (see Fig. 1, upper figure).

- Fig. 2B. average value of $B_x(y=0)$ Effect of $a_3=0$ is substantial to x=0.8".
- Fig. 3A. average value of $\partial B_y/\partial x$ (y=0) No effect from $b_4=0$. Again the situation is better than the ideal case up to $x\simeq 0.6$ " (see Fig. 1, lower figure).
- Fig. 3B. average value of $\partial B_{\chi}/\partial x$ (y=0) Effects of a_3 =0 are substantial to x = 0.8".
- Fig. 4A. standard deviation of ΔB_y (y=0) Fig. 4B. " B_x (y=0) Fig. 5A. " $\partial B_y/\partial x$ (y=0) Fig. 5B. " $\partial B_y/\partial x$ (y=0)

One may conclude from these figures that, with $b_4=0$ and $a_3=0$, the field flatness is extended from 0.3" to (0.6" \sim 0.7").

Can we tighten the criteria for b_4 and /or a_3 ?

Here I use 42 dipoles (one recently measured dipole added). If all other criteria are disregarded and

1. if $|a_3| < 2$ is strictly enforced, 30 pass 2. if $|a_3| < 1$ ", 14 pass 3. if $|b_4 - 1.| < 2$ ", 26 pass 4. if $|b_4 - 1.| < 1$ " 12 pass 5. if $|a_3| < 2$ and $|b_4 - 1.| < 2$ ", 16 pass 6. if $|a_3| < 1$ and $|b_4 - 1.| < 1$ ", 2 pass

What conclusion should be drawn from these numbers is not a very difficult question, I believe.









